

doublets, were obtained in absorption as in the table and in fig. 1. Several forbidden lines were observed. The greatest n measured and the intensity depended strongly upon the temperature.

	K, 4s-np	Rb, 5s-np	Cs, 6s-np
... ..	76	73	66
st	14	22	15

ON THE ENERGY LEVELS OF A MODEL OF THE COMPRESSED HYDROGEN ATOM

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Summary

In the problem of the "compressed hydrogen atom" the boundary condition that the wave function φ must be zero for infinite r , is replaced by the condition that φ must have a zero point at a finite $r = r_0$. This leads to an investigation of properties of the zeros of the confluent hypergeometric function. The shifts of the 1s, 2s and 2p levels by compression are calculated and tables and graphs are given for corresponding values of the energy and of r_0 .

§ 1. *Introduction.* In the usual treatment of the Schrödinger equation for the hydrogen atom the boundary conditions imposed on the wave function φ are: regular behaviour in the origin and a node at infinity. It will however be supposed here that the hydrogen atom is enclosed in a sphere of radius r_0 ^{1) 2)}. At the position r_0 is an infinitely high and steep potential wall. So the wave function must now have a zero point at $r = r_0$ instead of at $r = \infty$. The new boundary condition influences only the radial part $R(r)$ of the wave function. The equation for $R(r)$ can be written in atomic units^{*)}:

$$\frac{d^2 R}{dr^2} + \frac{2}{r} \frac{dR}{dr} + \left\{ 2E + \frac{2}{r} - \frac{l(l+1)}{r^2} \right\} R = 0, \quad (1)$$

with E the energy and l zero or a positive integer.

With the relations

$$\rho = 2r/n \text{ and } E = -1/2n^2, \quad (2)$$

*) Fundamental units e , m , and $\hbar = h/2\pi$. The unit of length is then $a_0 \equiv \hbar^2/me^2$ and the unit of energy is e^2/a_0 (Michéls, De Boer and Bijl¹⁾ take $e^2/2a_0$ as unit of energy).

REFERENCES

- Mack, Rev. Mod. Physics, **14**, 104, 1942.
Mack, Journ. Opt. Soc. Am. **32**, 457, 1942.